Measures of Location: First Moment

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# Introduction

Different aspects of a distribution of data can be summarised by the measures of location:

1. The First Moment: Middle.
2. The Second Moment: Spread.
3. The Third Moment: Symmetry.

All that being said, I would always recommend plotting the data first before anything else.

**A picture (histogram) is worth a thousand words.**

# First Moment: Middle

## Mean (average)

### Definition:

The mean , is the point around which the sum of the deviations is 0. The formula is given by

where is each element and is the number of elements. In words, add the numbers together and divided by how many numbers are in the list.

### Example

Given the list of 7 ages at a concert {19,18,20,18,18,18,20}, the mean is:

In R code:

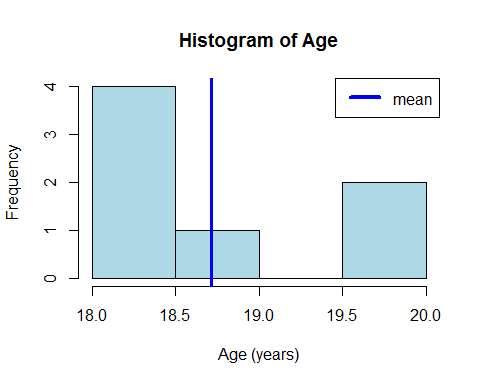
Age=c(20, 18,19, 18,18,18,20) # List of 7 numbers  
## Cacluate the mean in the long form  
(20+18+19+18+18+18+19+20)/7

## [1] 21.42857

## Cacluate the mean using the function mean  
mean(Age) # The mean of the list

## [1] 18.71429

### Graphical representation of the mean:



### Mean Pros and Cons

Pros of the mean:

* The mean is easy to calculate.
* The mean is well known and understood.

Cons of the mean: \* The mean is senstitive to extreme values.

Given the list of the ages of 8 people at a concert {20,18,19, 18,56, 18,18,20}, the mean is:

In R code:

Age=c(20,18,19, 18,56, 18,18,20) # List of 8 ages  
## Cacluate the mean using the function mean  
mean(Age) # The mean of the list

## [1] 23.375

## Median

### Definition:

The median is the middle values of an ordered list.

### Example

Given the list of 7 ages at a concert {19,18,20,18,18,18,20}.

1. First the list has to be ordered {18,18,18,18,19,20,20}.
2. Then the middle of the list found {18,18,18,*18*,19,20,20}.

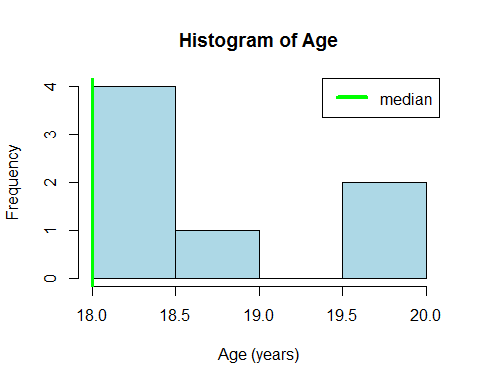
The median is 18.

In R code:

Age=c(20,18,19,18,18,18,20) # List of 7 numbers  
  
median(Age)

## [1] 18

### Graphical representation of the median:

 ### Median Pros and Cons Pros of the median:

* The median is the centre of the data - very intuitive.
* Not as sensitive as the mean to extreme values.

Cons of median: \* The calculation of the median does not use all data. \* Sorting a long list can be computationally expensive.

## Mode

### Definition:

The mode is the most commonly occurring value in the distribution.

### Example

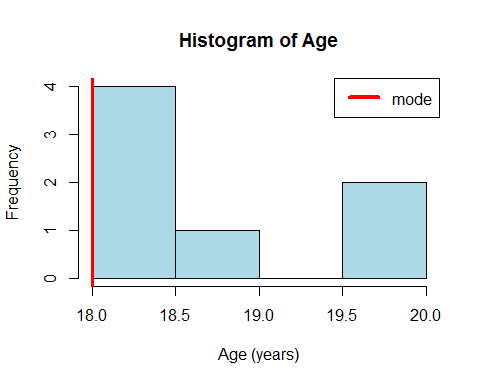
Given the list of 7 ages at a concert {19,18,20,18,18,18,20}. The most frequent values is 18, so 18 in the mode.

### In R code:

Age=c(20,18,19,18,18,18,20) # List of 7 numbers  
# Function to calculate mode  
Mode <- function(x) {  
 ux <- unique(x)  
 ux[which.max(tabulate(match(x, ux)))]  
}  
Mode(Age)

## [1] 18

### Graphical representation of the mode:



### Median Pros and Cons

Pros of the mode:

* The mode shows where the data is concentrated.

Cons of the mode:

* More than one Mode in a dataset.
* The calculation of the mode does not use all the data.

## All in one plot

The figure below shows a histogram of 3000 attendees age observations at a Wiggles concert: 